

SE(3) equivariance & invariance

SE(3), which represents the Special Euclidean Group in three dimensions, characterizes the rigid body motion in 3D space, including 3D translation and rotation.

Given an input point cloud $\mathcal{P} \in \mathbb{R}^{n \times 3}$, for any rotation matrix $R \in \mathbb{R}^{3 imes 3}$ and translation vector $T \in \mathbb{R}^3$. A SE(3) equivariant encoder \mathcal{E}_{equiv} means $\mathcal{E}_{inv}(\mathcal{P}R - \mathcal{P}R)$ and a SE(3) invariant encoder \mathcal{E}_{inv} means $\mathcal{E}_{equiv}(\mathcal{P}R+T)=\mathcal{E}_{equiv}(\mathcal{P})R+T$



EqvAfford: SE(3) Equivariance for Point-Level Affordance Learning

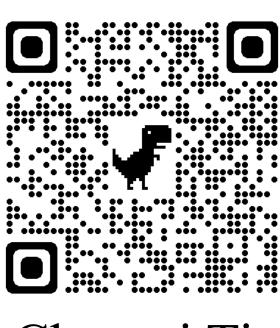
YueChen*, Chenrui Tie*, Ruihai Wu*, Hao Dong (* denotes equal contribution)

$$+\,T)={\cal E}_{inv}({\cal P})$$

Taking as input a point cloud of the object, our framework first outputs a per-point SE(3) invariant feature f_p^i and SE(3) equivariant feature f_p^e . The invariant f_p^i results in the affordance map invariant to object rotations, while the equivariant feature f_p^e results in the manipulation actions equivariant to object rotations.







Chenrui Tie

Links



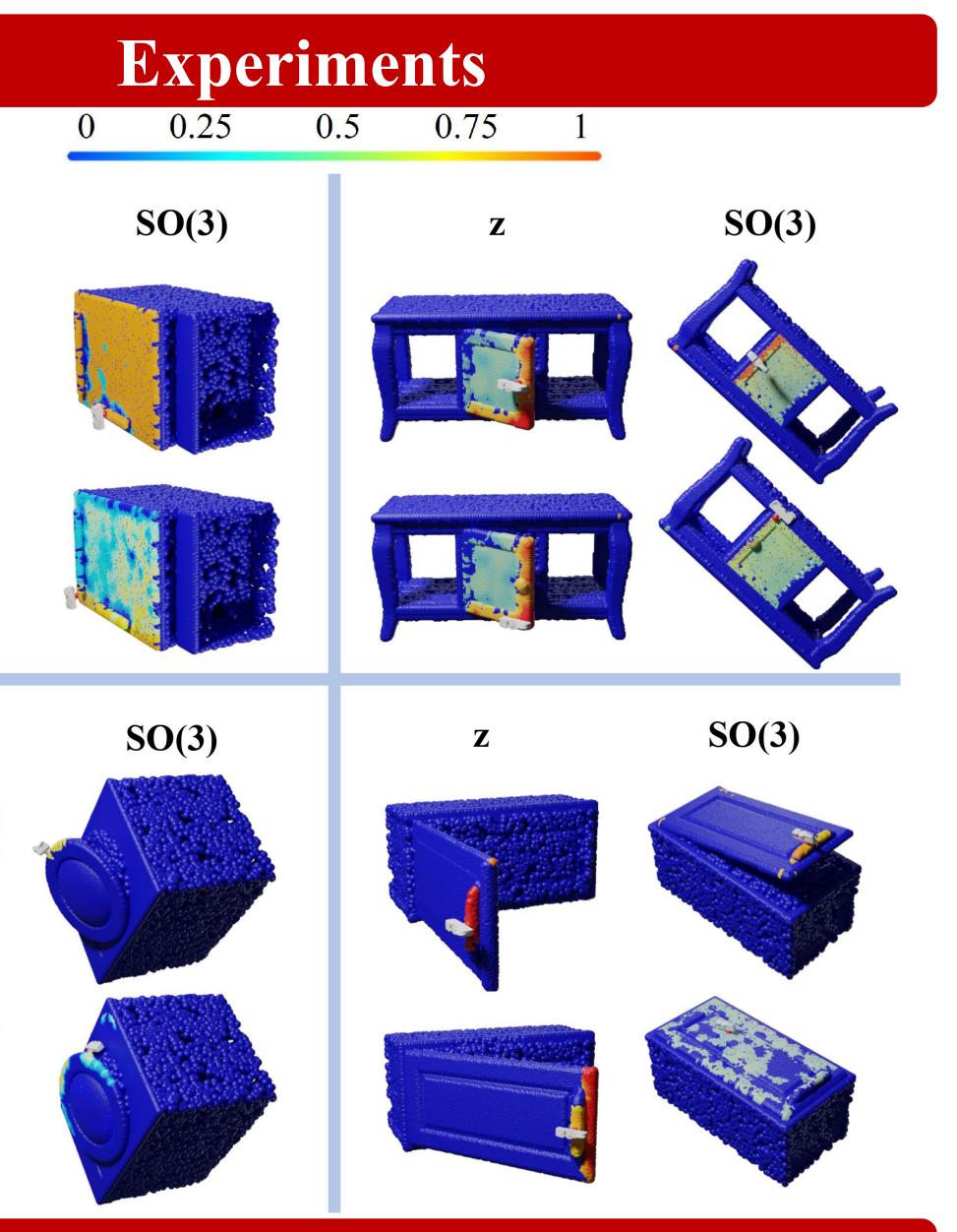


Hao Dong

We propose a novel framework, EqvAfford, leveraging SE(3) equivariance for affordance learning and downstream robotic manipulation with novel designs to theoretically guarantee equivariance. Predicting per-point SE(3) Invariant affordance and Equivariant interaction orientation, our method generalizes well to diverse object poses. Experiments on affordance learning and robotic manipulation showcases our method qualitatively and quantitatively.







Conclusion